

# The study of adjacent fault-tolerance for bipanclicity of hypercube

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## ABSTRACT

In this thesis, we investigate the adjacent vertices fault-tolerance for bipanclicity of hypercube. A bipartite graph  $G = (V, E)$  is bipancyclic if it contains the cycles of every even length from 4 to  $|V|$ . Let  $F_a$  be the set of  $f_a$  pairs of adjacent vertices and  $F_e$  be the set of  $f_e$  faulty edges in the  $n$ -dimensional hypercube  $Q_n$ . We will show that  $Q_n \setminus F_a \setminus F_e$  is bipancyclic for  $f_a + f_e = n - 2$ . A bipartite graph  $G = (V, E)$  is edge-bipancyclic if every edge of  $G$  lies on cycles of every even length from 4 to  $|V|$ . We will show that  $Q_n \setminus F_a \setminus F_e$  is edge-bipancyclic for  $f_a + f_e = n - 2, 0 \leq f_a \leq n - 3$ .

Keywords : hypercube, bipancyclic, edge-bipancyclic, fault-tolerant

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