

# 低雷諾數壓縮流場的紊流模式之改進

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## 摘要

本文主要是應用CFD(computational fluid dynamics)的方法，將低雷諾數壓縮流場的紊流模式與高雷諾數壓縮流場的紊流模式做一比較。在可壓縮流場的計算上，為了能準確的預估邊界層內複雜的情況，需選用適用性更廣的低雷諾數紊流模式，於是就採用了Chang and Hsieh 所發展出強健式低雷諾數紊流模式來進行流場的模擬。為了能充分解析層流次層 (viscous sublayer) 的變化，近壁處的格點分佈需非常細密，數值計算難度極高，所以在數值方法的選取及格點的產生極為重要。於數值方法中，本文在層流流場中選用了MUSCL Schem、LU-SSOR、時間前進法 (time marching)、有限體積等數值方法；在紊流流場中使用有限差分法，顯式法 (explicit) 疊代求解每一時間步驟 (time steps)，如此即可將紊流效應加入原流場的統御方程式之中，得到紊流效應的數值結果。而格點製作上，本文的幾何形狀為一個二維平板流場；格點採用正交交錯H型格點。因低雷諾數紊流模式的收斂情況需視邊界層內的格點數何近壁處的格點距離而定，所以需做疏密不同格點來比較，以期能找出於馬赫數大 (超音速流場) 也能收斂容易的格點。再將數值模擬的速度、阻力係數等流場性質與實驗值互相比較，希望能夠得到較好、令人滿意的低雷諾數壓縮流場的紊流模式。

關鍵詞：壓縮流場；紊流；強健式低雷諾數紊流模式；紊流模式

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