

Mycielski 圖形的環著色數上界

郭玟伶、黃鈴玲

E-mail: 9509866@mail.dyu.edu.tw

摘要

在尋找不含三角形且有任意大的著色數圖形時，Mycielski([15]) 發展出一種圖形轉換方式，可以將一個圖形 G 變形成一個新圖形 $M(G)$ ，稱之為 G 的 Mycielskian；重複此轉換，當 $t \geq 2$ 時，可以令 $Mt(G) = M(Mt-1(G))$ 。關於這些圖形之環著色數值(circular chromatic number; χ_c)的研究已經有一些發展。在這篇論文裡，我們主要探討的是 $\chi_c(Mt(G))$ 可能的範圍，特別是當 G 是完全圖(complete graph; K_n) 或環完全圖(circular complete graph; $K_{k,d}$) 時。Chang、Huang 及 Zhu 等人在 [3] 中證明了當 $\chi_c(G) \leq (G)-r$ 且 $r = 1/2$ 或 $1/3$ 時，可得到對任意正整數 t ， $\chi_c(Mt(G))$ 也會有 $\leq (Mt(G)-r)$ 的性質。我們進一步證明了此一性質在 $r = 2/3$ 時也會成立；換言之，當 $\chi_c(G)$ 接近 $\chi_c(G)-1$ 時， $\chi_c(Mt(G))$ 也會接近 $\chi_c(Mt(G))-1$ 。

關鍵詞：Mycielski 圖，環著色數

目錄

封面內頁 簽名頁 授權書.....	iii	中文摘要.....	iv	英文摘要.....	v
要.....	v	誌謝.....	vi	目錄.....	vii
目錄.....	ix	表目錄.....	x	1. Introduction	1.1. Basic definitions in graph theory1
				1.2. Circular chromatic number.....1	1.3. Mycielski graph3
				2. Preliminary results of $\chi_c(M(G))$	2.1 Graphs G with $\chi_c(M(G)) < \chi(M(G))$6
				2.2 Graphs G with $\chi_c(M(G)) = \chi(M(G))$7	2.3 Generalized Mycielski graphs8
				3. Upper bounds of d when $\chi_c(Mt(G)) = k/d$	3.1 The range of d when $\chi_c(Mt(K_n)) = k/d$11
				3.2 The range of d when $\chi_c(Mt(K_{k,d})) = k/d$12	4. The graphs $Mt(K_{k,d})$
				4.1. Graphs G with $\chi_c(G) \leq (\chi(G)-1)+1/3$16	4.2. Graphs G with $\chi_c(G) \geq \chi(G)-1/3$19
				5. Conclusions20	Reference21

參考文獻

- [1] H. L. Abbott and B. Zhou, The star chromatic number of a graph, *Journal of Graph Theory* 17 (1993), 349-360.
- [2] J. A. Bondy and P. Hell, A note on the star chromatic number, *Journal of Graph Theory* 14 (1990), 479-482.
- [3] G. J. Chang, L. Huang, and X. Zhu, Circular chromatic numbers of Mycielski's graphs, *Discrete Mathematics* 205 (1999), 23-37.
- [4] G. Fan, Circular chromatic number of Mycielski graphs, *Combinatorica* 24 (1) (2004), 127-135.
- [5] D. C. Fisher, Fractional colorings with large denominators, *Journal of Graph Theory* 20 (1995), 403-409.
- [6] D. C. Fisher, P. A. McKeena, and E. D. Boyer, Hamiltonicity, diameter, domination, packing and biclique partitions of Mycielski's graphs, *Discrete Applied Mathematics* 84 (1998), 93-105.
- [7] D. R. Guichard, Acyclic graph coloring and the complexity of the star chromatic number, *Journal of Graph Theory* 17 (1993), 129-134.
- [8] A. Gyarfás, T. Jensen, M. Stiebitz, On graphs with strongly independent color-classes, *Journal of Graph Theory* 46 (2004), 1-14.
- [9] H. Hajiabolhassan and X. Zhu, Circular chromatic number of subgraphs, *Journal of Graph Theory* 44 (2003), 95-105.
- [10] H. Hajiabolhassan and X. Zhu, Circular chromatic number and Mycielski construction, *Journal of Graph Theory* 44 (2003), 106-115.
- [11] L. Huang and G. J. Chang, The circular chromatic number of the Mycielskian of $G_{k,d}$, *Journal of Graph Theory* 32 (1999), 63-71.
- [12] P. C. B. Lam, W. Lin, G. Gu, and Z. Song, Circular chromatic number and a generalization of the construction of Mycielski, *Journal of Combinatorial Theory, Series B* 89 (2003), 195-205.
- [13] M. Larsen, J. Propp, and D. Ullman, The fractional chromatic number of Mycielski's graphs, *Journal of Graph Theory* 19 (1995), 411-416.
- [14] D. D-F. Liu, Circular chromatic number for iterated Mycielski graphs, *Discrete Mathematics* 285 (2004), 335-340.
- [15] J. Mycielski, Sur le coloriage des graphes, *Colloq. Math.* 3 (1955), 161-162.
- [16] E. Steffen and X. Zhu, Star chromatic numbers of graphs, *Combinatorica* 16 (1996), 439-448.
- [17] C. Tardif, Fractional chromatic numbers of cones over graphs, *Journal of Graph Theory* 38 (2001), 87-94.
- [18] A. Vince, Star chromatic number, *Journal of Graph Theory* 12 (1988), 551-559.
- [19] X. Zhu, Star chromatic numbers and products of graphs, *Journal of Graph Theory* 16 (1992), 557-569.
- [20] X. Zhu, Circular chromatic number: a survey, *Discrete Mathematics* 229 (2001), 371-410.