

# 超立方體可扇形化相鄰點容錯之研究

陳俐宏、黃鈴玲

E-mail: 9509834@mail.dyu.edu.tw

## 摘要

在本篇論文中，我們要介紹與研究超立方體圖形的相鄰點容錯後的可扇形化性質。我們將證明 $n$  階超立方體錯 $f$  對相鄰點， $l$  條邊後是 $(n-f-l)^*$ -fanable 當 $n$  大於等於3， $f+l$  小於等於 $n-2$ ， $f$  小於等於 $n-3$ 。另外我們更進一步證明 $n$  階超立方體在壞掉一點的情況下，錯 $f$  對相鄰點， $l$  條邊後是 $(n-f-l-1)^*$ -fanable 當 $n$  大於等於3， $f+l$  小於等於 $n-2$ ， $f$  小於等於 $n-3$ 。

關鍵詞： $n$  階超立方體，可扇形化。

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