

Heuristic Approaches for Solving Two-dimensional Packing Problems

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ABSTRACT

Two-dimensional packing and cutting problems are a kind of common tasks encountered by industries, such as shoes making, textile, steel, clothing, etc. Although the cost of each industrial material is not the same, its cost occupies sizable proportion in the total cost. Therefore, finding an effective permutation method becomes one of the most important goals of them. In this study, we propose a simulated annealing (SA) based algorithm - IBH2, revised from the IBH algorithm appeared in the open literature for packing rectangle boxes with different sizes in material plates. IBH2 was developed using the placement policy of IBH, while adopting a new SA mechanism allowing the temperature increasing during the annealing process. In addition, we entered the concept of parallel processing and proposed a parallel simulated annealing (PSA). The performance of IBH2 and PSA were verified by running several benchmarking problems and the results were reported. Experimental results indicate that IBH2 and PSA are capable to offer robust and efficient solutions.

Keywords : packing problems, simulated annealing, parallel processing

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REFERENCES

- [1] 張幼蘭, 「動態平行模擬退火法」, 清華大學工業工程學系碩士班碩士論文, 2002。
- [2] 田邦廷, 「長方體物件排列問題解法之研究」, 大葉大學工業工程學系碩士班碩士論文, 2002。
- [3] 陳璋昶, 「平行模擬退火法之改進」, 清華大學工業工程學系碩士班碩士論文, 2003。
- [4] 陳其揚, 「使用平行模擬退火演算法於功能性核磁共振造影像分析之研究」, 大葉大學工業工程學系碩士班碩士論文, 2004。
- [5] 吳泰熙、駱景堯、林東養, 「多尺寸方形排列問題啟發式解法之研究」, 工業工程學刊, 第17卷, 75-85, 2000。

- [6] 鄭守成, 「MPI 平行計算程式設計」, 國家高速電腦中心, 2001。
- [7] Aarts, E., Bont, J., and Laarhoven, P. " Parallel implementations of the statistical cooling algorithm, " *Integration*, 4, pp.209-238 (1986).
- [8] Aarts, E. and Korst, J. " Simulated annealing and boltzmann machines, " *Wisely*, New York, USA, (1989).
- [9] Azencott, " Simulated Annealing:Parallelization Techniques, " *Wisely*, (1992).
- [10] Babu, A.R. and R. Babu, " Effective nesting of rectangular parts in multiple rectangular sheets using genetic and heuristic algorithms, " *International Journal of the Production Research*, 37, pp.1625-1643 (1999).
- [11] Beasley, J. E., " Algorithms for unconstrained two-dimensional guillotine cutting, " *Journal of the Operational Research Society*, 36, 297-306 (1985).
- [12] Biro, M. and E. Borors, " Network flows and non-guillotine cutting patterns, " *European Journal of Operational Research*, 16, pp.215-221 (1984).
- [13] Chen, C. S., S. Sarin, and B. Ram, " The pallet packing for non-uniform box sizes, " *International Journal of Production Research Society*, 29, 1963-1968 (1991).
- [14] Christofides, N. and C. Whitlock, " An algorithm for two dimensional cutting problems, " *Operations Research*, 25, 30-44 (1977).
- [15] Dagli, C. H. and A. Hajakbari, " Simulated annealing approach for solving stock cutting problem, " *IEEE Transactions on Systems, Man, and Cybernetics*, pp.221-223 (1990).
- [16] Dagli, C. H. and M. Y. Tatoglu, " An approach to twodimensional cutting stock problem, " *International Journal Production Research*, 25, pp.175-190 (1987).
- [17] Dowsland, K. A. and W. Dowsland, " Packing problem, " *European Journal of Operational Research*, 56, 2-14 (1992).
- [18] Dowsland, K. A. " Some experiments with simulated annealing techniques for packing problems, " *European Journal of Operational Research*, 68, 389-399 (1993).
- [19] Gilmore, P. C. and R. E. Gomory, " A linear programming approach to the cutting stock problem (Part 1), " *Operations Research*, 9, 849-855 (1961).
- [20] Gilmore, P. C. and R. E. Gomory, " A linear programming approach to the cutting stock problem (Part 2), " *Operations Research*, 11, 863-888 (1963).
- [21] Gilmore, P. C. and R. E. Gomory, " A linear programming approach to the cutting stock problem (Part 2), " *Operations Research*, 11, 863-888 (1963).
- [22] Goulimis, C., " Optimal solution for the cutting stock problem, " *European Journal of Operational Research*, 44, 197-208 (1990).
- [23] Hopper, E. and B. C. H. Turton, " An empirical investigation of meta-heuristic and heuristic algorithms for a 2D packing problem, " *European Journal of Operational Research*, 128, pp34-57, (2001).
- [24] Ismail, H. S. and K. K. B. Hon, " The nesting of 2-dimensional shapes using genetic algorithm, " *Proceedings of the Institution of Mechanical Engineers Part B-Journal of Engineering Manufacture*, 209, 115-124 (1995).
- [25] Jakobs, S., " On genetic algorithms for the packing of polygons, " *European Journal of Operational Research*, 88, pp165-181 (1996) [26] Kirkpatrick, S., C. D. Gelatt. Tr., and M.P. Vecchi, " Optimization by simulated annealing, " *Sci.*, 22, 671-680 (1983).
- [27] Lai K. K. and J. W. M. Chan, " Developing a simulated annealing algorithm for the cutting stock problem, " *Computers ind. Engng.*, 32, No.1, pp.115-127 (1997).
- [28] Leung T.W. , C. H. Yung, and D. M. Troutt, " Applications of genetic search and simulated annealing to the two-dimensional non-guillotine cutting stock problem, " *Computer and Industrial Engineering*, 40, pp.201-214 (2001).
- [29] Leung T.W. , C. K. Chan, and D. M. Troutt, " Application of a mixed simulated annealing-genetic algorithm heuristic for the two-dimensional orthogonal packing problem, " *European Journal of Operational Research*, 145, pp.530 – 542 (2003).
- [30] Nader, N. and Z. Saeed, " Adaptive temperature control for simulated annealing: a comparative study, " *Computers & Operations Research*, 31, 2439-2451 (2004).
- [31] Pacheco, P. S., " Parallel Programming With MPI, " *University of San Francisco*, (1995).
- [32] Ram, D. J., T. H. Sreenivas. and K. G. Subramaniam, " Parallel simulated annealing algorithm, " *Journal of Parallel and Distributed Computing* , 37, pp.207-212 (1996).
- [33] Wu, T. H., J. F. Chen, C. Y. Low, and P. T. Tang, " Nesting of two-dimensional parts in multiple plates using hybrid algorithm, " *International Journal of the Production Research*, 41, 3883-3900 (2003).
- [34] Yu G. S. and V. N. Patsuk, " A method of optimal lattice packing of congruent oriented polygons in the plane, " *European Journal of Operational Research*, 124, 204-216 (2000).