

# 無人自行車之動態模擬與控制

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## 摘要

在本篇論文中，以Lagrange's equations的方式來推導腳踏車之動態方程式，以系統之動態方程式來考慮地面和兩輪純滾動之限制條件，每一輪的微分疊代方程式都有兩個完整和兩個非完整限制條件，把所有的限制條件以向量形式轉換為Jacobian矩陣，並討論以疊代法搜尋腳踏車之平衡點，當中也提出如何計算輪胎與地面接觸的曲率半徑和參考點之比較。為要求解動態的DAEs和確定模擬數值解之精確性，文中也提到如何處理限制條件之計算方法。從動態模型的建立，到PID和模糊控制器之建立，並產生把手轉動力矩使得傾倒的腳踏車可以重新再為持平衡，然而再利用另一個模糊控制器控制腳踏車到想要的平衡點，在保持平衡時，腳踏車會維持在一個參考的滾動角，並且以腳踏車與參考軌跡的最短距離及腳踏車前進的方向來計算控制量，因此無人騎乘的腳踏車會跟隨地面的軌跡移動，由模擬結果可以知道這方法是可行的。最後，使用基因演算法來訓練模糊控制器於多變的控制任務，像自我平衡、滾動角跟隨和軌跡跟隨，模擬結果顯示這個方法有非常快速的訓練效果，在幾代的疊代後，就可以產生極佳的控制參數，使控制器有極好的控制性能。

關鍵詞：腳踏車動態方程式，多體，數值穩定，模糊控制，路徑跟隨，腳踏車之穩定，基因演算法。

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