

# Edge Fault-tolerant Hamiltonian Laceability of Bipartite Hypercube-like Networks

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## ABSTRACT

The edge fault tolerance for Hamiltonian properties of  $n$ -dimensional bipartite hypercube-like graphs  $X_n$  are explored. The main result of this thesis is that  $X_n - F$  is Hamiltonian laceable where  $F$  is the faulty edge set with  $|F| = n-2$ , and hyper-Hamiltonian laceable with  $|F| = n-3$ .

Keywords : hypercube-like, Hamiltonian laceable, hyper-Hamiltonian laceable, fault-tolerant.

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