

# Bifanability of Bipartite Hypercube-like Networks

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## ABSTRACT

In this thesis, we introduce the concepts of bifanability and fault tolerant bifanability. We show that the  $n$ -dimensional hypercube  $Q_n$  and bipartite hypercube-like  $X_n$  are  $f$  edges fault tolerant  $k^*$ -bifanable for  $n \geq 3, 0 \leq f \leq n-2, 1 \leq k \leq n-f$ . We also prove that the  $n$ -dimensional hypercube  $Q_n$  is  $f$  edges fault tolerant  $k^*$ -bifanable with one faulty node for  $n \geq 3, 0 \leq f \leq n-3, k=n-f-1$ .

Keywords : super bifanability, fault tolerant bifanability, hypercube, bipartite hypercube-like

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