

# Exact Tsallis Random Number Generator with its Applications and Ramifications in the Optimization of Continuous Function

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## ABSTRACT

Tsallis distribution was proposed by C. Tsallis in 1996 to solve the slow convergence problem of simulated annealing. It is shown that Tsallis' s generalized simulated annealing is much faster than the classical simulated annealing ( " Boltzmann machine " ) and fast simulated annealing ( " Cauchy machine " ). However, Tsallis distribution is very complicated and its random variable could not be generated by ordinary simulation techniques such as inversion and rejection methods. Tsallis distribution has two parameter  $q$  and  $T$ . We standardize the Tsallis distribution by setting  $T=1$ . When  $T$  not equal to 1 we use the linear transform to transform standardized Tsallis distribution. The standardized Tsallis distribution can be simulated as follow. When  $q > 1$  it is Normal distribution. When  $1 < q < 1$

Keywords : Ratio of uniform、GSA、Tsallis distribution、random number generator、generalized simulated annealing、convex enveloping polygon

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