

以四為基底之心脈式RSA加解密系統晶片

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摘要

基於改善蒙哥馬利的演算法，我們提出了適用於RSA 公開金鑰密碼系統的位元階層之心脈式陣列。在指數演算法中，我們使用插入平方運算與乘法運算的方式，使得乘法器的使用率可以達到 100%。以修改過的布斯演算法為基礎，我們設計與實現了一個以四為基底之位元插入心脈式陣列的RSA 密碼系統。藉由減少迭代的運算次數，以及管線化的技術，我們的RSA 密碼系統比傳統的方法要快上四倍，且運算一筆 512 位元的RSA 運算只需要大約平均 0.26M 個時脈週期，其RSA 密碼系統加解密的速度在工作頻率為 333M Hz 時可達到 656 Kb/s。

關鍵詞：心脈式；密碼系統；蒙哥馬利

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