

# 一般化煎餅網路之環狀容錯研究

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## 摘要

在本篇論文中，我們研究n-dimensional 2-sided pancake graphs ( $2P_n$ )的容錯性質。其中當 $n \geq 3, F \subseteq V(2P_n) \subseteq E(2P_n)$ ,  $|F| = (n-2)$ 時,  $2P_n - F$ 為漢米爾頓圖形(Hamiltonian graphs)，而當 $|F| = (n-3)$ 時,  $2P_n - F$ 為漢米爾頓連通圖 (Hamiltonian connected graphs)。此外，我們並更進一步研究n-dimensional m-sided pancake graphs ( $mP_n$ ) 的容錯性質。我們推論假如  $mP_2$  是2-漢米爾頓圖形 與 1-漢米爾頓連通圖，在此前前提下則可驗證在 $n \geq 3, m \geq 3, F \subseteq V(mP_n) \subseteq E(mP_n)$ , 當 $|F| = (2n-2)$ 時,  $mP_n - F$ 為漢米爾頓圖形，而當 $|F| = (2n-3)$ 時,  $mP_n - F$ 為漢米爾頓連通圖。

關鍵詞：煎餅網路；容錯；漢米爾頓路徑；漢米爾頓迴路；漢米爾頓連通圖

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