

NURBS應用於損壞影像修復及影像壓縮之研究

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摘要

“ Non-Uniform Rational B-Splines ” 非均勻有理仿曲線一般簡稱為NURBS，由於NURBS具有完整的數學架構，因此被廣為採納而制訂成國際標準，在CAD/CAM及電腦繪圖等領域被廣泛應用。在2-D數位影像中可以視為NURBS的3-D曲面，因此我們將它應用在影像處理上。絕大多數的B-Spline應用在影像內插，直到1997年T. Watanabe提出以B-Spline的數學架構作為影像壓縮，爾後1999年J. W. Park and S. U. Lee利用B-Spline的內插的特性將它應用在影像修補上。然而Park and Lee ' s 未能適當的找出節點(knot vector)及控制點(control points)。為了解決這方面的缺點，我們使用bi-variate NURBS曲面以解決影像上修補及壓縮的問題。在這我們提出單一隱藏層的類神經架構來決定3-D NURBS曲面所需的控制點，而實驗證明我們所提出的方法能得到較佳的結果。

關鍵詞：非均勻有理仿曲線

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