

以四基底之高速RSA加解密系統晶片

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摘要

現在已經進入了數位通訊的時代，大量的商業活動和個人信件，都經由網際網路來傳遞，因此資料保密、身分認證、數位簽署等安全需求便日益重要。RSA是1978年美國麻省理工學院 (MIT) 三位教授Rivest、Shamir及Adleman首先提出一種基於分解因數的指數函數密碼系統，為目前使用最廣泛的公開金鑰密碼系統。在RSA公鑰密碼系統中，每個使用者都擁有兩把鑰匙——公鑰與私鑰。公鑰公布給所有的人知道，私鑰則由自己秘密保存著。公鑰密碼系統的安全性在於幾乎無法由公鑰計算推導出私鑰，也就是靠這種計算不可行性 (computational infeasibility) 才得以保密。假如藉計算推導確實不易取得私鑰，那麼我們可以稱這系統是安全的。RSA密碼系統就是利用大數因數分解相當困難的這個事實來製造公鑰與私鑰。基於安全性，隨著計算機技術的進步，金鑰的長度也不斷的增加。因RSA編解碼需做大量運算，當金鑰長度大於500位元時，比較適合以硬體來處理，以減低系統的負擔。本論文提出一個以四為基底的模乘法演算法，我們改善蒙哥馬利 (Montgomery) 演算法來設計模乘法器，並應用此模乘法器去實現一個 512 位元的 RSA 公開金鑰密碼系統晶片。本設計用 Avant! 0.35 μ m standard cell library 來合成電路，並送至 CIC (國家晶片系統設計中心) 製作雛形晶片。本系統面積約六萬閘，當工作在 150 MHz 時脈時平均有 196 Kbits/sec 的速率。

關鍵詞：蒙哥馬利演算法；公開金鑰密碼系統；模乘法

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