# 植基於橢圓曲線密碼系統的數之研究

# 劉作屏、陳澤雄

E-mail: 9127189@mail.dyu.edu.tw

### 摘要

本篇論文研究的主題包含有數位簽章及代理簽章兩個部分。其中有關數位簽章的部分,目前的數位簽章機制都是建立在公開金鑰密碼系統上,也就是說每位簽章者都只能擁有一把密鑰及一把公鑰。從安全性來看,這樣的機制是不夠安全的,因為這把密鑰一但被攻擊者破解出來,其後果是不堪設想的。因此,我們提出了一種新的機制,使得每位簽章者可以同時用兩把密鑰及一把公鑰來做數位簽章的動作。此時的攻擊者除非能同時破解出這兩把密鑰,否則只有破解出其中一把密鑰時,而本機制仍然是安全的。 這樣的機制,可以應用到數位簽章的機制上,以提高其安全性。 至於代理簽章的部分,在許多已提出的代理簽章機制中,原始簽章者與代理簽章者之間通常需要一個安全的管道來傳遞授權參數,以達到授權代理的目的。為了必免安全管道的需求,學者 ZHANG 提出了一個採用交談式的代理簽章機制。所謂交談式是指原始簽章者與代理簽章者之間有一些參數的往返,這樣的授權方式明顯較浪費頻寬且沒有效率。因此,我們提出了一種有別於ZHANG且不需安全管道就能達到 授權代理目的之代理簽章機制。此外,本研究還採用了橢圓曲線密碼系統作為數位簽章機制的架構,橢圓曲線密碼系統的相關研究近年來相當為人矚目。從安全性及有效性來看,這種密碼系統有著重要的應用前景,是一種可能在近期內某些方面取代RSA或DSS等現存的密碼系統,現已逐漸形成了研究的重點。這種密碼系統的誘人之處在於安全性相同的前提下,可使用較短的密鑰金鑰,一般認為,在Q位元域上的橢圓曲線密碼系統,當Q的長度為160位元時,其安全性卻相當於RSA使用1024位元模數,密鑰金鑰較短意味著所需要電腦網路的頻寬和記憶體較小,這在電腦網路應用中有時候是個決定性的關鍵。因此藉由橢圓曲線密碼系統短金匙特性的應用,本研究提出新的數位簽章系統,用以提昇安全機制的效能。

關鍵詞:數位簽章、代理簽章、資訊安全、密碼學、橢圓曲線密碼系統

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