

# Curve Skeleton Extraction Using Directional Distance Transform

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## ABSTRACT

Curve-skeletons are a simply representation of complex objects and are useful for many visualization tasks including virtual navigation, animation, medical image, etc. There are many algorithms in the literature describing extraction methodologies. Many of them still have different unsolved problems, and few algorithms allow users to determine different levels of skeletons. In this thesis, we present a curve-skeleton extraction algorithm using directional distance transform, whose basic idea is to mimic the water flow to locate feature points. For each pixel, the shortest distance to boundaries is determined first. If two or more pixels on the boundaries are within the distance, a compact angel and a vector of water-flow direction are also determined. Such a pixel is called a feature point. A curve-skeleton can be obtained by connecting these feature points, and then pruning the result. We also build a software platform for experimental purposes. The user can set different parameters to extract skeletons in different abstraction levels. The preliminary results indicate that our algorithm is orientation-independent and can produce better skeletons than existing methods.

Keywords : medial axis transform、curve-skeleton、directional distance transform、digital image processing

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