

# The study of the adjacent vertices fault-tolerance for two spannability of star graphs

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## 摘要

在連結網路中Star graph 是一個耳熟能詳的拓樸網路架構。Sn 是n 維星狀圖。此論文中探討星狀圖二可生成性質相鄰點容錯。在Sn 上兩條路徑P1和P2是兩條跨越不相交路徑。先令Fe 是Sn 上壞邊的集合和Fav 是Sn 上相鄰壞點對數的集合。我們要證明的是在Sn 上, Sn - Fe - Fav 時有 Fe + Fav ≤ n - 4, 再任給2 對不同顏色的點s1, s2 ∈ V0 和 t1, t2 ∈ V1, 我們能找到兩條路徑把所有的點都走完, 而且互不相交。

關鍵詞：星狀圖、跨越不相交路徑、邊容錯、相鄰點容錯

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