

# 複合材料型樑之熱回彈行為探討

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## 摘要

本研究針對碳纖維複合材料疊層型樑由固化至成形時，因溫度效應所造成之變形現象進行探討，並藉由疊層順序來降低應用在複合材料L型樑上所產生之熱回彈量。因此，本研究之主要目的開發一解析解預測模型，該預測模型以2D型態計算出包含疊層順序、疊層厚度、折彎半徑與設計角度之影響因素所產生熱回彈角，並應用有限元素法（Finite Element Method）之商業套裝軟體ANSYS以3D模型來模擬長度與疊層偏差，探討造成熱回彈角與具反對稱（Antisymmetric）、擬向性（Quasi-isotropic）等疊層角度所產生扭曲量。本文也應用ANSYS來模擬驗證解析解之熱回彈角，以驗證數學模型具一折彎半徑之複合材料L型樑、U型樑固化成形後產生之熱回彈角（Spring-in）及其疊層順序之影響，並探討其疊層厚度、疊層偏差、折彎半徑以及長度等製造參數與熱回彈角、扭曲（Twist）及翹曲（Warpage）關係，以期能提供操作人員了解各種加工參數對於熱回彈角的影響程度，並作為一修正加工參數的參考依據。進一步將所得之結果與解析解模型、實驗結果比較，以驗證此解析解模型之可行性與準確性。利用連續回彈，尋找模具最佳補償角，製造工程師以此製造符合欲成形角度之複合材料L型樑，以降低修整模具比例，進而減少成本與時間的浪費，最後使用MATLAB開發一介面系統整合全部流程，提供預測成形角度更有效率。

關鍵詞：複合材料型樑、固化翹曲、熱回彈角、有限元素法

## 目錄

封面內頁	簽名頁	授權書	iii	中文摘要	iv	英文摘要	v	誌謝	vi	目錄	vii	圖目錄	x	表目錄	xiii	第一章 緒論	1	1.1 研究背景與動機	2	1.1.1 纖維材料疊層順序與熱翹曲之關係	4	1.1.2 纖維與樹脂材料性質和熱翹曲之關係	5	1.1.3 成型溫度影響熱翹曲	5	1.2 研究目的	6	1.3 研究方法	6	第二章 文獻回顧	11	2.1 複合材料熱效應	11	2.2 古典層板理論	12	2.2.1 平板位移與應變	13	2.2.2 正交機械性質組成	15	2.3 Reisser - Mindlin一階剪切變形理論	19	2.4 濕熱效應	20	2.5 電腦輔助模擬與分析	26	第三章 研究方法	27	3.1 材料性質檢測	28	3.1.1 試片製作	28	3.1.2 拉伸實驗	35	3.1.3 熱膨脹係數檢測	37	3.2 複合材料L型樑熱回彈之數學模型	38	3.3 電腦輔助模擬與分析	40	3.3.1 元素設定	41	3.3.2 有限元素模型	43	3.3.3 邊界條件設定	50	3.4 實驗方法	53	3.5 逆向工程	54	3.6 熱回彈補償與設計角度修正	56	3.7 模具之最佳化設計	57	3.8 ANSYS與MATLAB的結合與應用	59	第四章 結果與討論	61	4.1 複合材料之機械性質	61	4.2 TMA試驗結果	64	4.3 新解析解之結果探討	65	4.3.1 新解析解之改良探討	65	4.3.2 實驗與解析解及模擬值比較結果	66	4.3.3 邊界條件比較結果	69	4.4 材料與製程參數於熱回彈影響之探討	70	4.4.1 熱膨脹係數差異與熱回彈之關係	70	4.4.2 材料疊層角度與熱回彈之關係	72	4.4.3 疊層偏差與熱回彈之關係	75	4.4.4 折彎半徑與熱回彈之關係	78	4.4.5 疊層厚度與熱回彈之關係	79	4.4.6 結構長度與熱回彈之關係	81	4.4.7 設計角度與熱回彈之關係	84	4.5 模具補償角最佳化之探討	86	4.6 MATLAB預測系統之開發	88	第五章 結論與未來發展方向	90	5.1 結論	90	5.2 未來發展方向	91	參考文獻	92	附錄A 模型回彈角計算方法	96
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## 參考文獻

- [1] Czaderski C. and Motavalli M., " Fatigue behaviour of CFRP L-shaped plates for shear strengthening of RC T-beams, " Composite, vol. 35, pp. 279-290, 2004.
- [2] Gigliotti M. et al., " Development of curvature during the cure of AS4/8552 [0/90] unsymmetric composite plates, " Composites Science and Technology, vol. 63, pp. 187-197, 2003.
- [3] Fernlund G. et al., " Experimental and numerical study of the effect of cure cycle, tool surface, geometry, and lay-up on the dimensional fidelity of autoclave-processed composite parts, " Composites, vol. 33, pp. 341-351, 2002.
- [4] Oliveira B.F. and Creus G.J., " Nonlinear viscoelastic analysis of thin-walled beams in composite material, " Thin-Walled Structures1, vol. 41, pp. 957-971, 2003.
- [5] Jones R. and Alesi H., " On the analysis of composite structures with material and geometric non-linearities, " , Composite Structures, vol. 50, pp. 417-431, 2000.
- [6] Bapanapalli S.K. and Smith L.V., " A linear finite element model to predict processing-induced distortion in FRP laminates, " Composite, vol. 36, pp. 1666-1674, 2005.
- [7] Bapanapalli S.K. and Smith L.V., " An experimental investigation on mechanisms for manufacturing induced shape distortions in

homogeneous and balanced laminates, " Composite, vol. 32, pp. 827-838, 2001.

[8]Alam M. K. and Angheliescu M. S., " Analysis of Deformation and Residual Stresses in Composites Processed on a Carbon Foam Tooling, " Journal of Composite Materials, vol. 43, pp. 2057-2070, 2009.

[9]Fernlund G., Floyd A., " Process analysis and tool compensation for curved composite L-angles, " Canadian-International Composites Conference, vol. 6, 2007.

[10]Dong C., Zhang C., Liang Z., Wang B., " Dimension variation prediction for composites with finite element analysis and regression modeling, " Composites, vol. 35, pp. 735-746, 2004.

[11]Bhagwan D. Agarwal, Lawrence J. Broutman, Analysis And Performance of Fiber Composites, 1990.

[12]Laszlo P. Kollar, George S. Springer, Mechanics of Composite Structures, Cambridge University Press, pp. 436-452, 2003.

[13]Chen D., Cheng J., Reinforced Plastics and Composites, vol. 12, pp. 1323-1339, 1993.

[14]Philippidis, T. P. J., Composite Materials, vol. 28, pp. 252-261, 1994.

[15]Radford, D.W. and Diefendorf, R.J., " Shape Instabilities in Composite Resulting from Laminate Anisotropy, " Journal of Reinforced Plastics and Composites, 12 ( 1 ) , pp.58-75, 1993.

[16]Dong C., " Modeling the process-induced dimensional variations of general curved composite components and assemblies, " Composites, vol. Part A 40, pp. 1210-1216, 2009.

[17]G. Fernlund, " Spring-in of angled sandwich panels, " Composites Science and Technology, vol. 65, 317-323, 2005.

[18]Mindlin. R. D. " Influence of Rotatory Inertia and Shear on Flexural Motions of isotropic, Elastic plate, " Journal of application Mechanics, vol. 18, pp. 31-38, 1951.

[19]Hsiao K.-T. and Gangireddy S., " Investigation on the spring-in phenomenon of carbon nanofiber-glass fiber /polyester composites manufactured with vacuum assisted resin transfer molding, " Composite, vol. 39, pp. 834-842, 2008.

[20]Radford D.W., " volume fraction gradient induced warpage in curved composite plates, " Composite Engineering, vol. 5, pp.923-934, 1995.

[21]Lalit K. Jain, Meng Hou, Lin Ye and Yiu-Wing Mai, " Spring-in study of the aileron rib manufactured from advanced thermoplastic composite, " Composite, vol. 29, pp. 973-979, 1998.

[22]Albert C., Fernlund G., " Spring-in and warpage of angled composite laminates, " Composites Science and Technology, vol. 62, pp. 1895-1912, 2002.

[23]Alam M. K., Angheliescu M. S., " Analysis of Deformation and Residual Stresses in Composites Processed on a Carbon Foam Tooling," Journal of Composite materials, vol. 43, pp. 2057-2070, 2009.

[24]Wiersma H. W., Peeters L. J. B., Akkerman R., " Prediction of spring-forward in continuous-fibre /polymer L-shaped parts, " Journal of Composite materials, vol. 29A, pp. 1333-1342, 1998.

[25]Feih S., Shercliff H.R., " Quality assessment of curved composite components in peel joint structures, " Composites, vol. 36, pp. 397-408, 2005.

[26]Jung W.-K., Kim B., Won M.-S., Ahn S.-H., " Fabrication of radar absorbing structure ( RAS ) using GFR-nano composite and spring-back compensation of hybrid composite RAS shells, " Composite Structures, vol. 75, pp. 571-576, 2006.

[27]Salomi A., Garstka T., Potter K., Greco A., Maffezzoli A., " Spring-in angle as molding distortion for thermoplastic matrix composite, " Composites Science and Technology, vol. 68, pp. 3047-3054, 2008.

[28]ASTM Standards, ASTM D3039/D3039M-8, " Standard Test Method for Tensile Properties of Polymer Matrix Composite Materials. "

[29]王正賢, 郭文雄, 賴宏智, 賴居廷, 謝承諺, 陳育德, 林永崑, " 複合材料L型樑固化翹曲之研究探討, " 中華民國航空太空學會第五十一屆全國學術研討論文集, pp. 242-242, 2009 [30]王正賢, 謝承諺, 賴?民, " 複合材料L型樑熱翹曲預測模型之推導, " 中華民國力學學會第三十四屆全國力學會議, pp. 242-242, 2010