

The study of adjacent vertex-fault-tolerance for two spanning disjoint paths of hypercube

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ABSTRACT

We investigate the adjacent vertex fault-tolerance for two spanning disjoint path of hypercube in this thesis. We propose two results as follows. Let F_a be the set of $|F_a|$ pairs of adjacently faulty vertices and F_e be the set of faulty edges of Q_n . Let s_1, s_2, t_1, t_2 be four distinct fault-free vertices of $Q_n = (V_b \cup V_w, E)$ for $s_1, t_1 \in V_b$ and $s_2, t_2 \in V_w$. There exist two spanning disjoint paths $P(s_1, t_1)$ and $P(s_2, t_2)$ of $Q_n - F_a - F_e$ with $|F_a| \leq n - 4$ and $|F_a| + |F_e| \leq n - 3$. Let $F_v \subseteq V_b$ be a set of two faulty vertices of Q_n . Let $s_1, s_2, t_1, t_2 \in V_w$ be four distinct fault-free vertices of Q_n . There exist two spanning disjoint paths $P(s_1, t_1)$ and $P(s_2, t_2)$ of $Q_n - F_a - F_v$ with $|F_a| \leq n - 4$.

Keywords : hypercube、adjacently faulty vertices、fault-tolerance、two spanning disjoint paths

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